## USN

## Fourth Semester B.E. Degree Examination, June/July 2013 Field Theory

Time: 3 hrs. Max. Marks: 100

Note: Answer FIVE full questions, selecting at least TWO questions from each part.

## PART - A

- 1 a. State and explain Coulomb's law of force between the two point charges. Also indicate the units of quantities in the force equation. (05 Marks)
  - b. State and apply Gades law to obtain an expression for the electric field intensity due to an infinite sheet of charge with a surface charge density  $\rho$ ,  $C/m^2$  and area A  $m^2$ . (10 Marks)
  - c. Find: i) Electric field intensity and ii) Electric flux density at the origin due to  $Q_1 = 0.35 \,\mu\text{C}$  at (0, 4, 0) m and  $Q_2 = -0.55 \,\mu\text{C}$  at (3, 0, 0) m. (05 Marks)
- 2 a. Explain with mathematical expressions: i) Potential difference ii) Absolute potential iii) Potential gradient. (06 Marks)
  - b. Derive an expression for the equation of continuity of current.

(06 Marks)

- c. At the boundary between glass ( $\leq$  4) and air, the lines of electric field make an angle of 40° with normal to the boundary. If electric flux density in air is 0.25  $\mu$ C/m<sup>2</sup>, determine the orientation and magnitude of, i) Electric flux density and ii) Electric field intensity, in glass. (08 Marks)
- 3 a. Derive Poisson's and Laplace equations starting from point form of Gauss law. (06 Marks)
  - b. Using Laplace equation derive an expression for the capacitance of a concentric spherical capacitor. The inner spherical conductor is of radius 'a' and potential V, while outer conductor is of radius 'b' and potential zero. (08 Marks)
  - c. Determine whether or not the following potential fields satisfy Laplace's equation:

i) 
$$V = 2x^2 - 3y^2 + z^2$$

ii) 
$$V = r^2 + z^2$$

(06 Marks)

4 a. Write an explanatory note on Biot Savarts law.

(04 Marks)

- b. Discuss the concept of scalar and vector magnetic potential and arrive at the expressions for Poissons equation in magnetostatics. (08 Marks)
- c. State and prove ampere's circuital law and apply it to a straight solid conductor to calculate the magnetic field intensity. (08 Marks)

## PART - B

- 5 a. Find the expression for the force on differential current carrying elements. (06 Marks)
  - b. Define Lorentz force equation and mention the application of its solution. (06 Marks)
  - c. Calculate the inductance of a Solenoid of 200 turns wound tightly on a cylindrical tube of length 60 cm and of diameter 6 cm, with air as media. Derive the expression used. (08 Marks)

- 6 a. With necessary relationships, explain Faradays law of electromagnetic induction for both static and time varying conditions. (10 Marks)
  - b. Starting from Faradays law of electromagnetic induction derive  $\nabla \times \vec{E} = -\frac{\partial \vec{B}}{\partial t}$ . (06 Marks)
  - c. Find the frequency at which conduction current density and displacement current density are equal in a medium with  $\sigma = 2 \times 10^{-4}$  s/m and  $\epsilon_r = 81$ . (04 Marks)
- 7 a. What is uniform plane wave? Explain its propagation in free space with necessary equation.
  (08 Marks)
  - b. Define skin depth and depth of penetration.

(08 Marks)

- c. For copper the conductivity is 58 mega-s/m. Find the skin depth at a frequency of 10 MHz.

  (04 Marks)
- 8 a. With necessary equations, explain standing wave ratio.

(10 Marks)

b. Find weather the wet, marshy soil characterized by σ = 10<sup>-2</sup> s/m, ∈<sub>r</sub> = 15 and μ<sub>r</sub> = 1 may be considered as a conductor, a dielectric or neither for the frequencies: i) 60 Hz
 ii) 1 MHz
 iii) 100 MHz
 iv) 10 GHz.
 (10 Marks)